

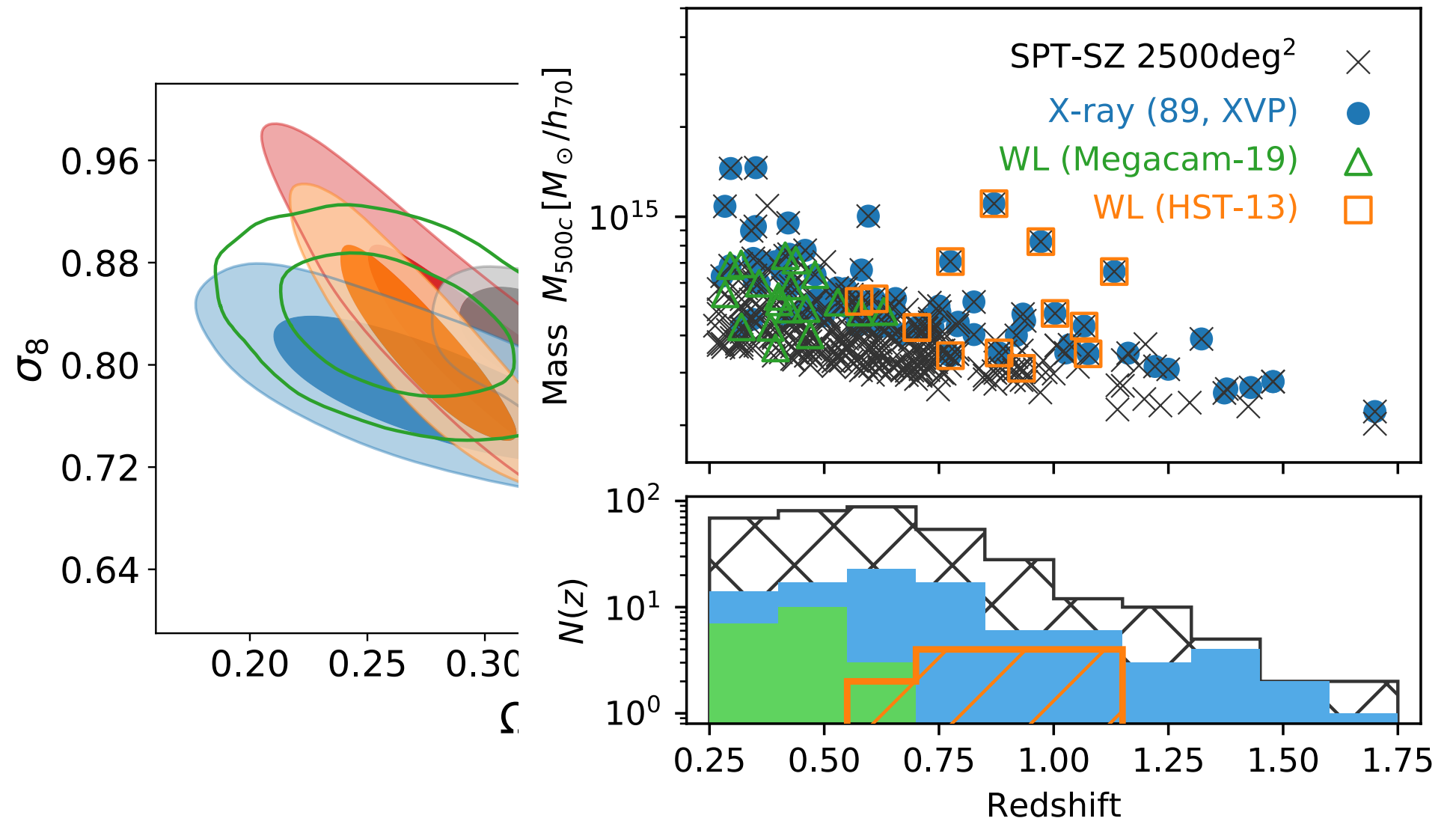
# Weak-Lensing Calibrated Cluster Cosmology



Sebastian Bocquet - LMU Munich

# LCDM with varying sum of neutrino masses

Bocquet et al. [2019ApJ...878...55B](#)



**How did we get here?**

# Premise: Modeling Framework

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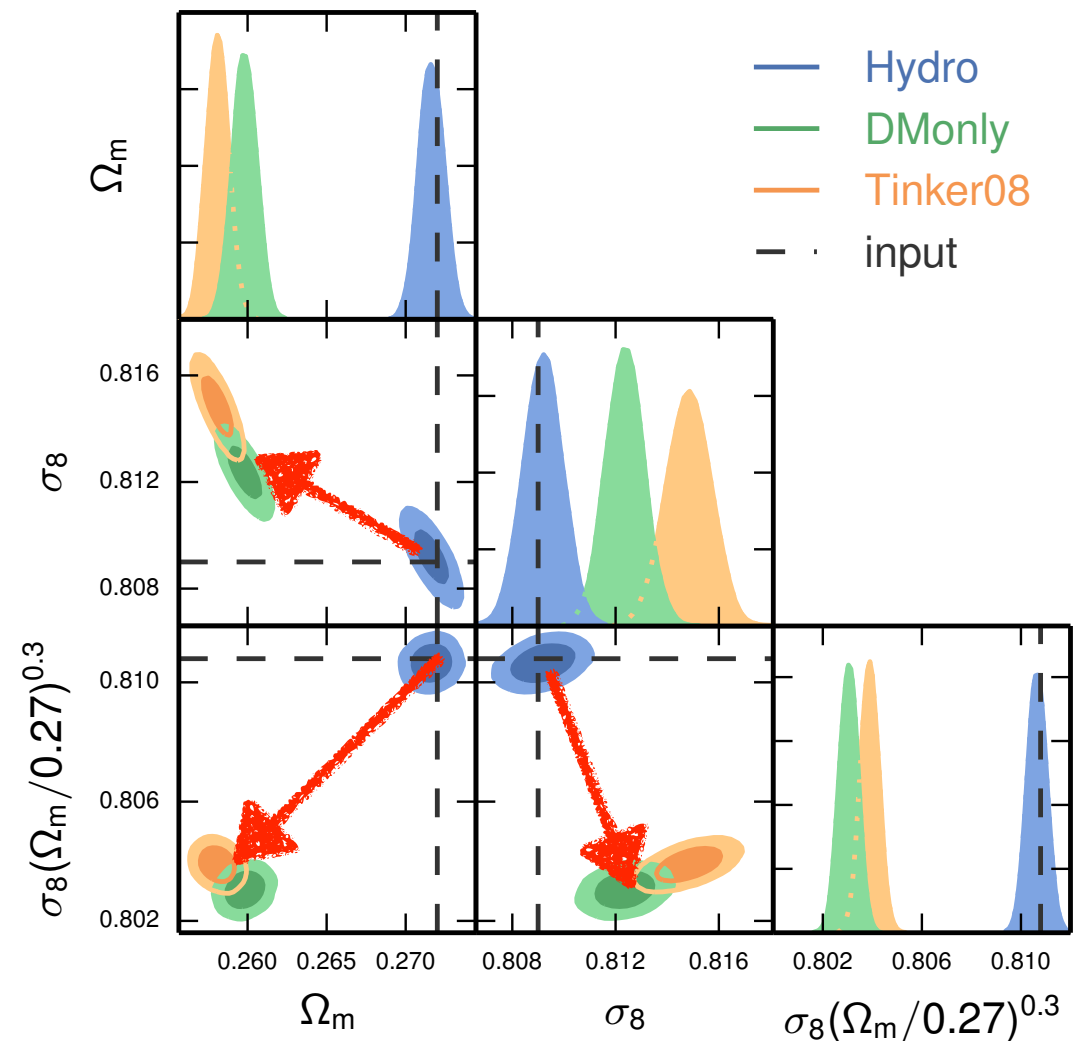
- Cluster cosmology is a modeling challenge.
- Be explicit about your assumptions!
- **We will not**
  - assume hydrostatic equilibrium
  - consider a hydrostatic bias extracted from hydro simulations (yet?)
- **We will** trust our intuition (and decades of research) that
  - cluster mass proxies correlate with mass
  - Mean observable—mass relation is well described by a power law in mass and redshift (with unknown parameters)
  - weak gravitational lensing measures halo mass with %-level systematic uncertainty (calibrated against numerical simulations because we don't have perfectly centered NFW-profile halos)
  - We should account for correlated scatter between the different observables (correlation is introduced, e.g., by projecting onto the plane of the sky)
- Theory prediction for halo abundance from  $N$ -body simulations (Tinker+08)

# Baryons and the Halo Mass Function

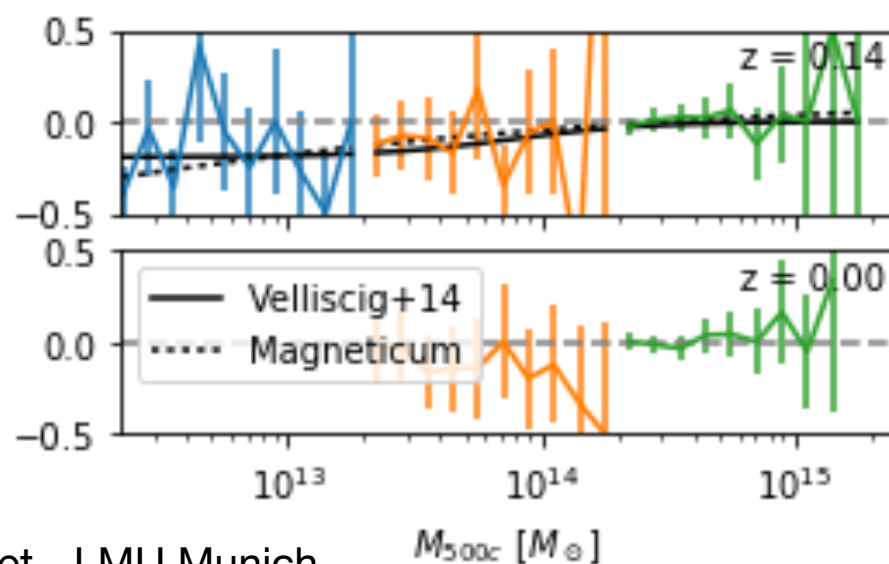
Bocquet et al. 2016, MNRAS 456, 2361



- At fixed halo mass, feedback processes change the abundance
- Use hydrodynamical *Magneticum Pathfinder* simulation suite (Dolag et al., [www.magneticum.org](http://www.magneticum.org))
- Up to  $(2688 \text{ Mpc}/h)^3$  to sample high-mass halos
- Hydro effects are important for upcoming studies using  $M < \sim 1e14 \text{ Msun}$

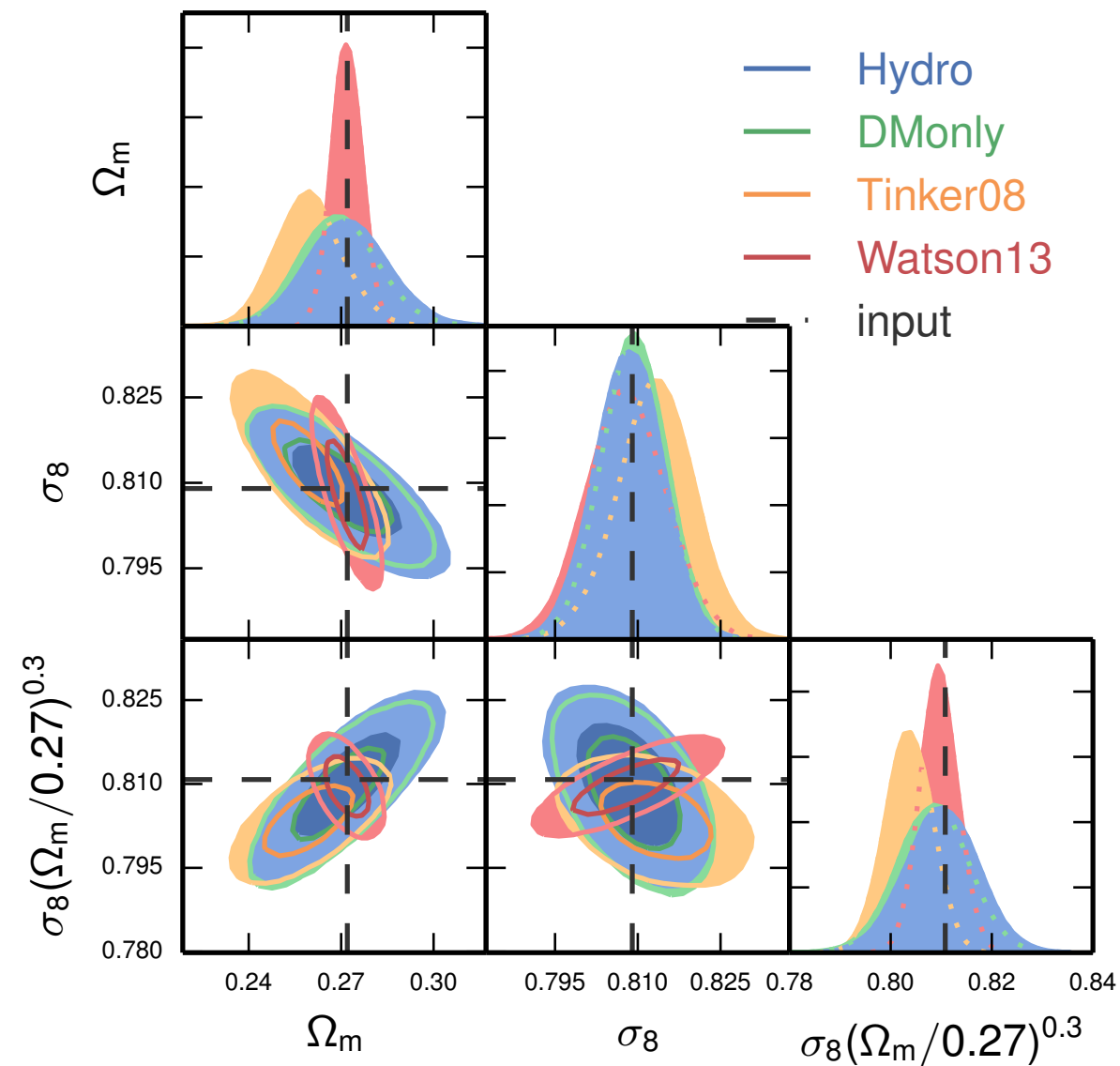


**Biases if effect of hydro is ignored for eROSITA-like surveys with  $M > 7e13 \text{ Msun}$**



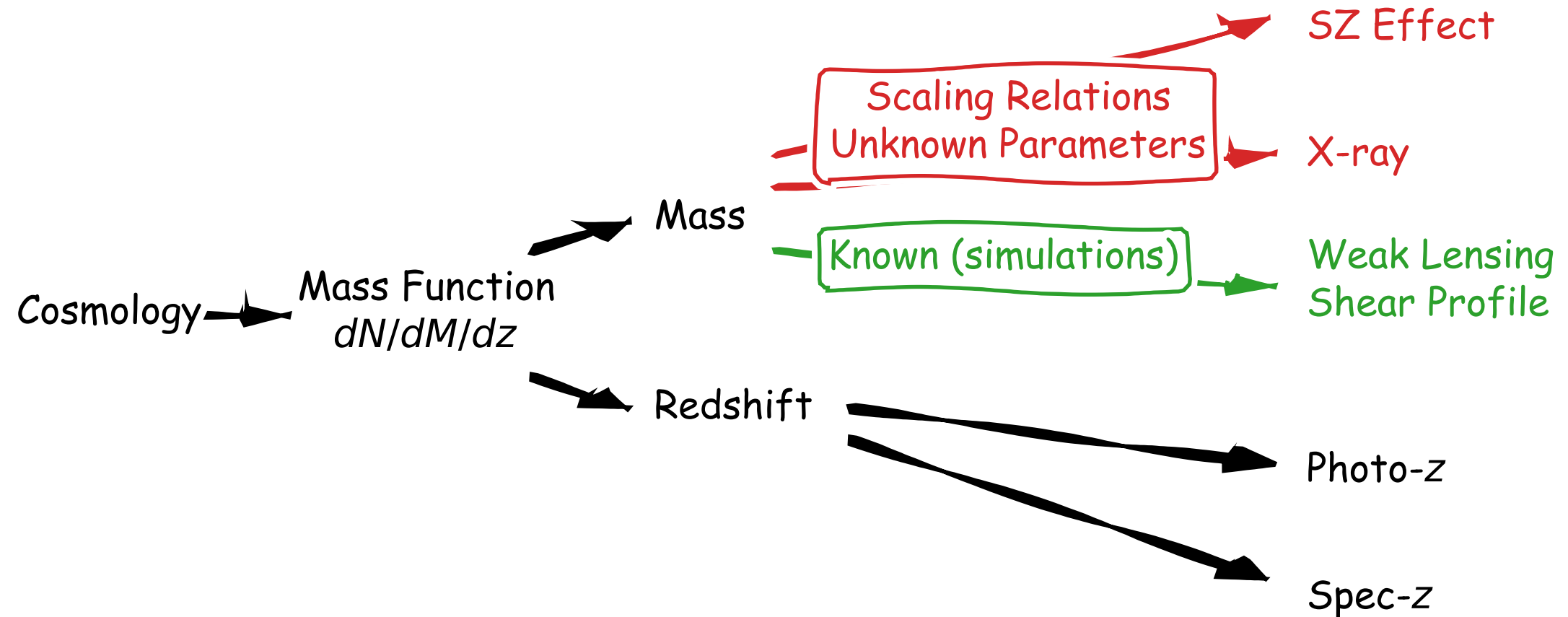
# Impact of Feedback on HMF for SPT: None?

Bocquet et al. 2016, MNRAS 456, 2361



***Magneticum Pathfinder* hydro simulations (Dolag et al.)**

# Forward-Modeling Analysis Strategy



Use the known relation  
**mass -> weak lensing shear profile**  
to calibrate  
**mass -> SZ effect** and **mass -> X-ray**

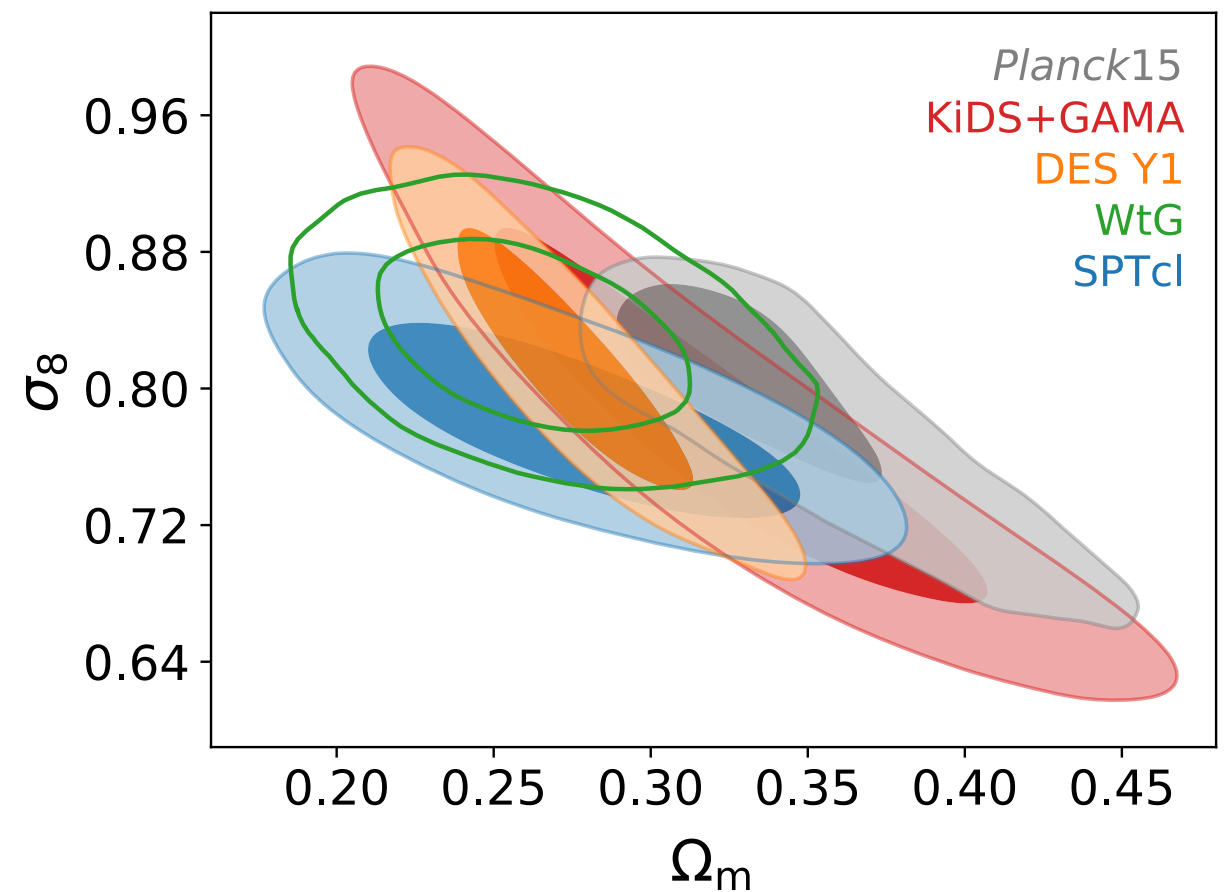
**Simultaneous analysis of all observables and cosmology to capture all covariances**

# LCDM with varying sum of neutrino masses

Bocquet et al. [2019ApJ...878...55B](#)



- Wide flat priors on SZ scaling relation parameters fully encompass posterior
- Cluster constraint statistically limited by mass calibration: need more (weak lensing) data! (currently 32 clusters)
- $1.5\sigma$  agreement with *Planck*15 TT+lowTEB



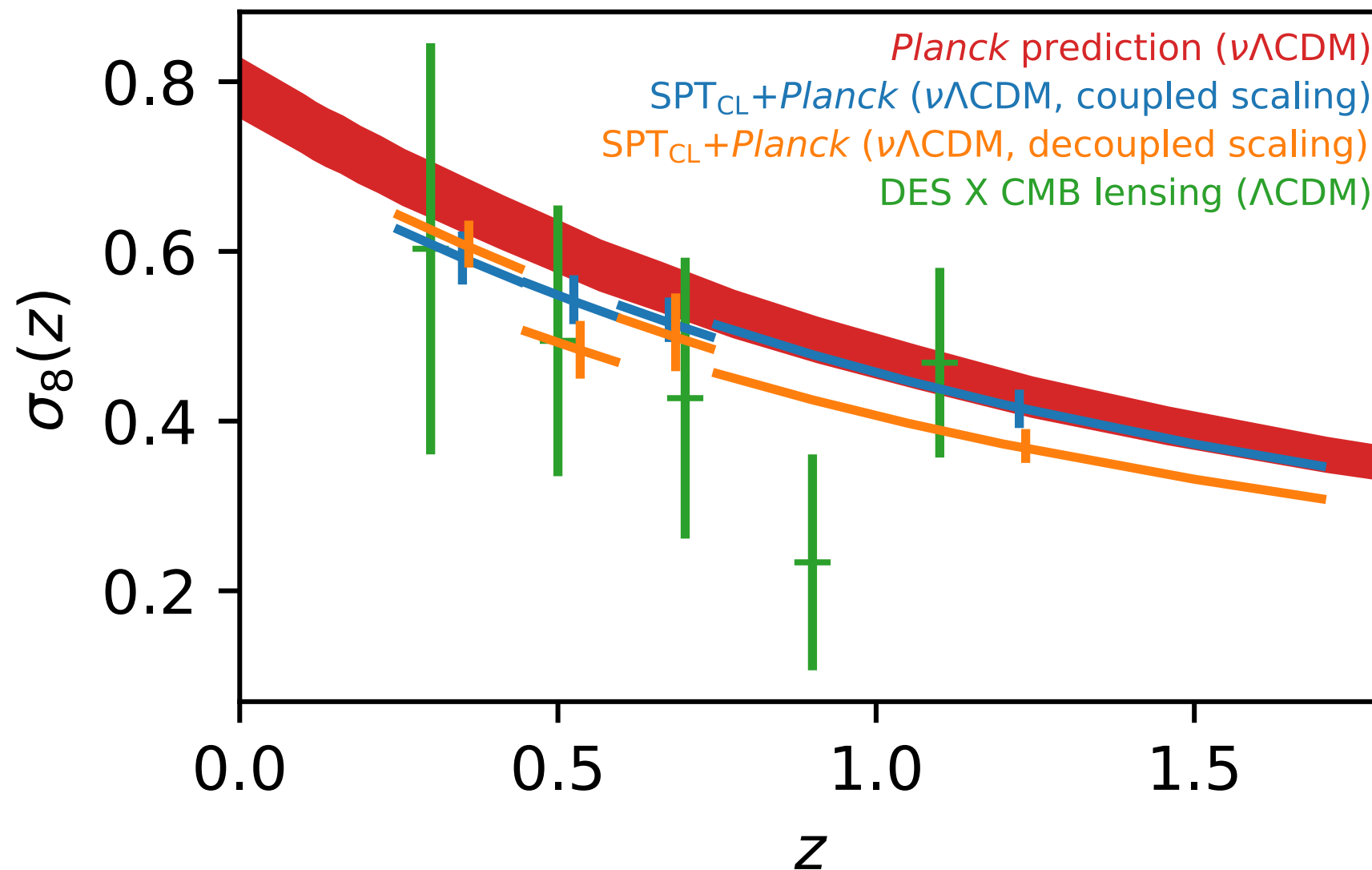
# Linear Growth of Structure

Bocquet et al. [2019ApJ...878...55B](#)



**Blue error bars:** *Planck* constrains the geometry of the Universe only, clusters constrain growth.

**Orange error bars:** More freedom in observable – mass relation



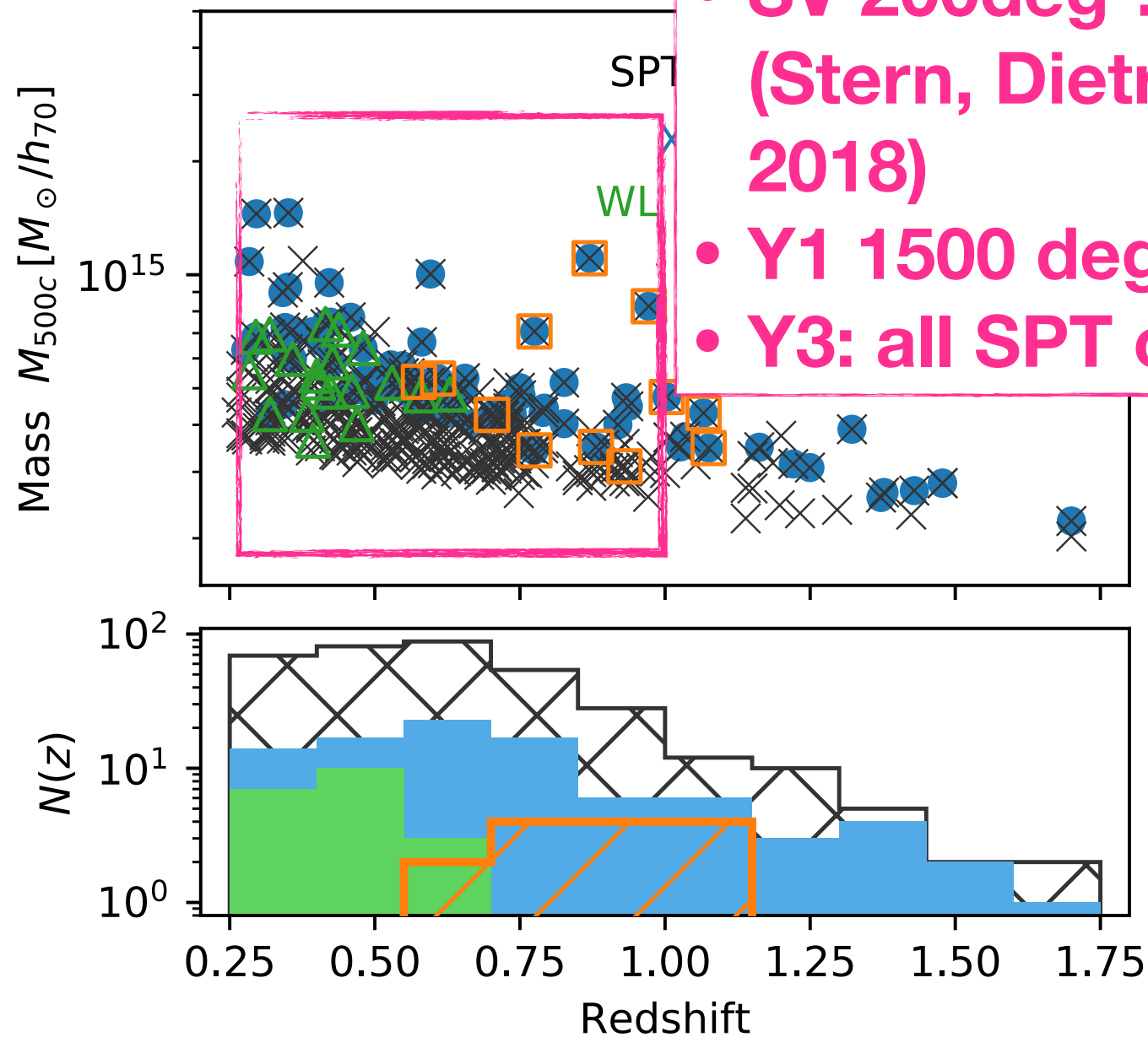
**How are we going to improve?**

# The Dark Energy Survey

- CTIO Blanco Telescope
- 5000 square degrees in *grizy*
- Survey is complete — analysis of Y3 data ongoing
- Strategically overlaps the SPT survey



# SPT Clusters + DES Weak Lensing



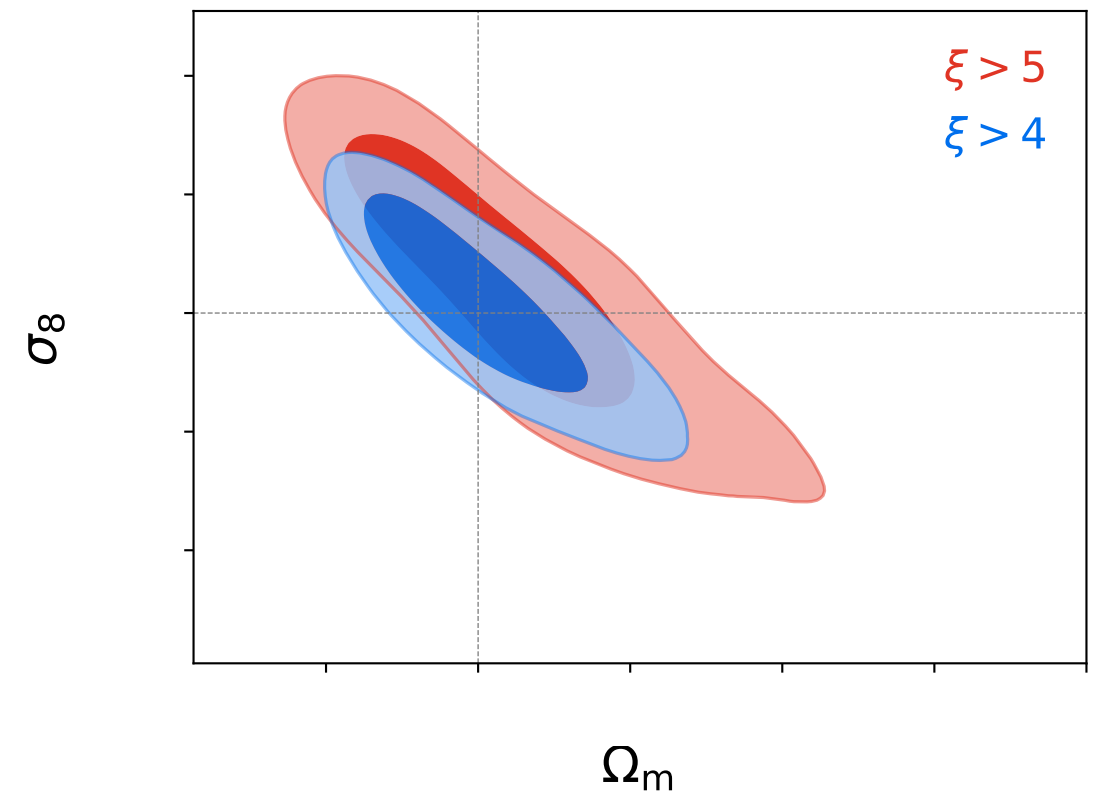
## WL calibration from DES

- SV 200deg<sup>2</sup>: 34 clusters (Stern, Dietrich, Bocquet+ 2018)
- Y1 1500 deg<sup>2</sup>
- Y3: all SPT clusters  $z < 1$

# SPTcluster + DES WL Analysis Pipeline

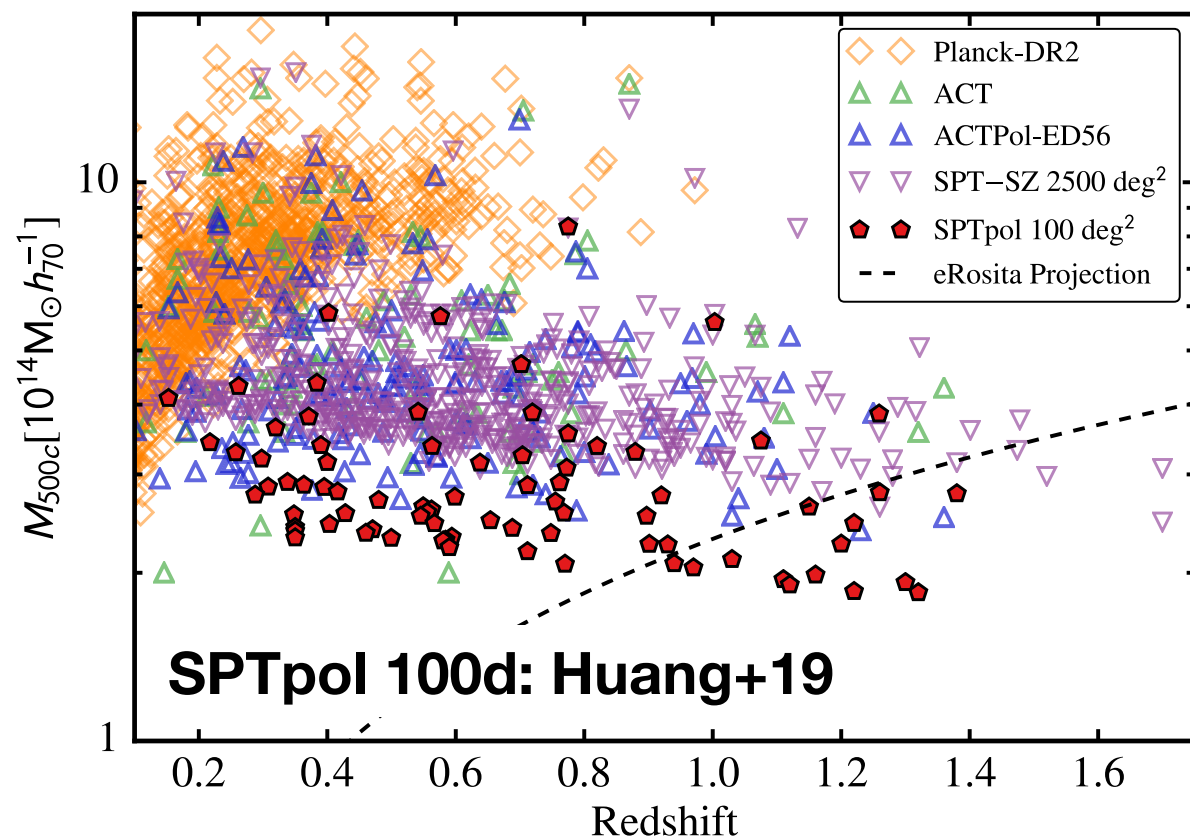


- Opportunity to make several improvements
  - Better cluster member contamination correction (Maria Paulus, Joe Mohr)
  - Explicitly marginalize over halo concentration for each halo
  - Forward-model lensing miscentering (more flexibility)
- Pipeline validation against full-scale mocks
- Data analysis will be performed blindly



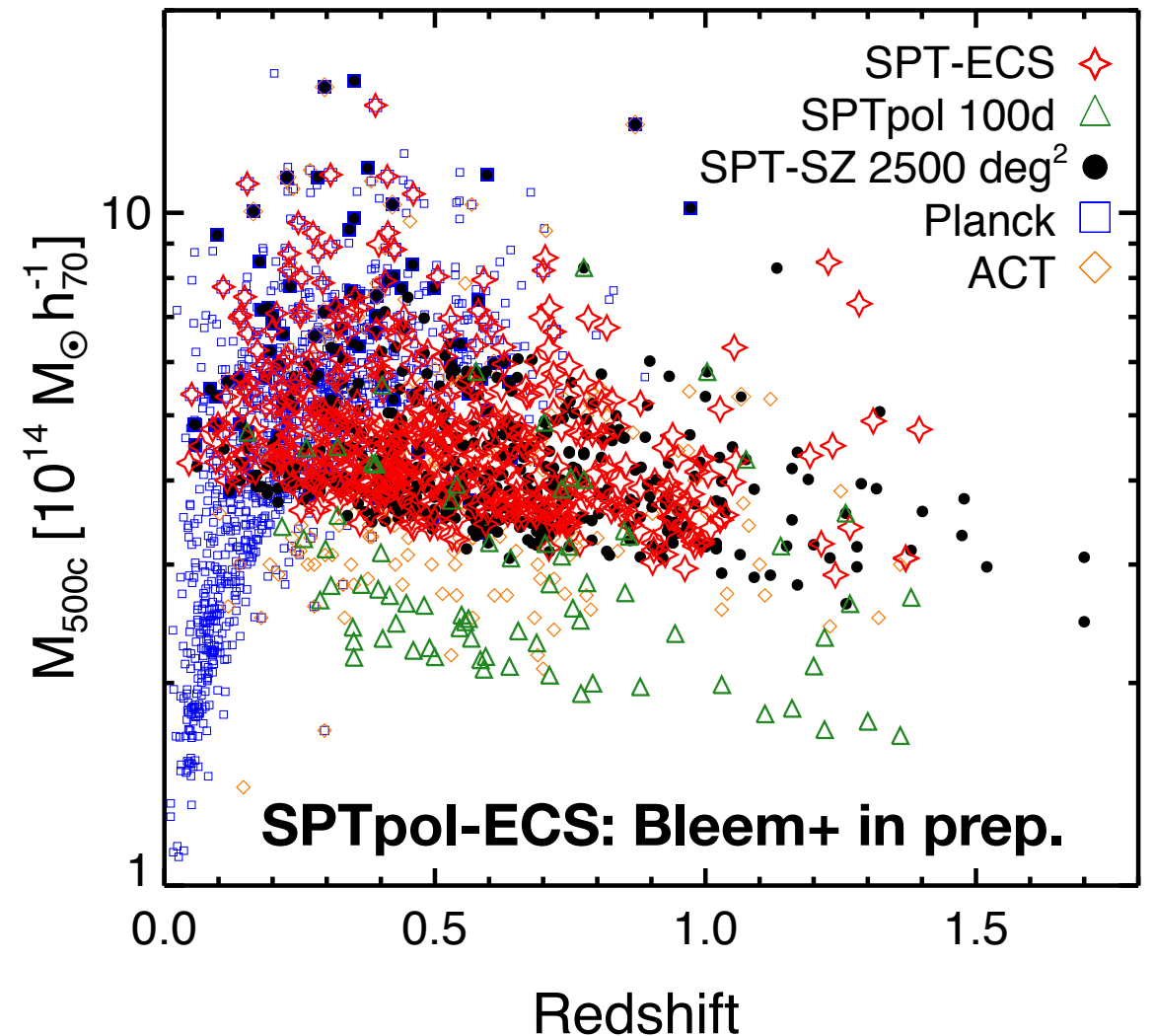
Pipeline validation against  
complete mocks  
(Bocquet+ in prep.)

# Clusters in the SPTpol Survey



## SPTpol 100d “deep field”

- 3–4x deeper than SPT-SZ
- deeper = lower-mass clusters
- ~1 cluster per deg<sup>2</sup>



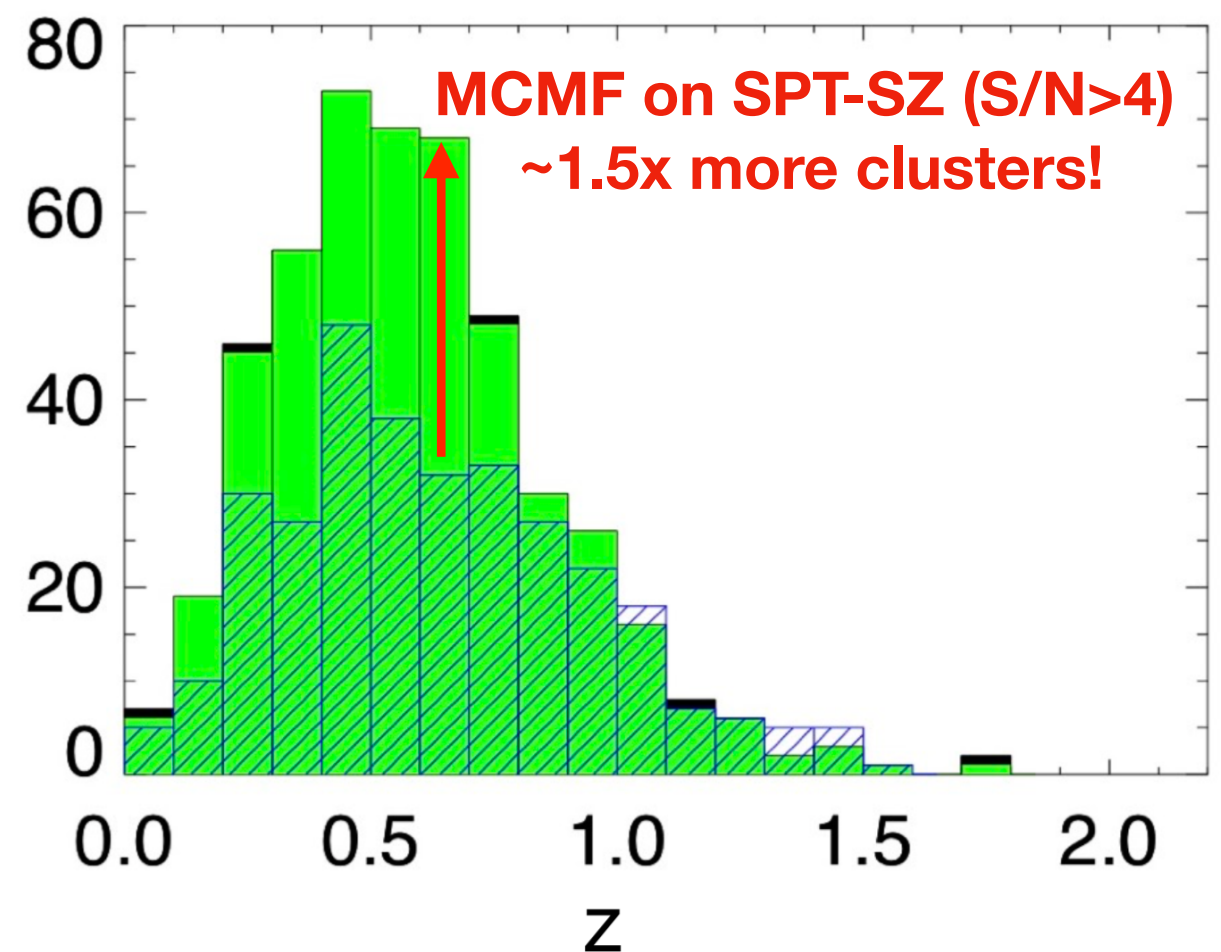
## SPTpol 2700d “Extended Cluster Survey”

- ~*Planck* depths
- Brings total number of SPT clusters to >1000

# Better Exploitation of SZ Data: Multi-Component Matched Filter (MCMF)



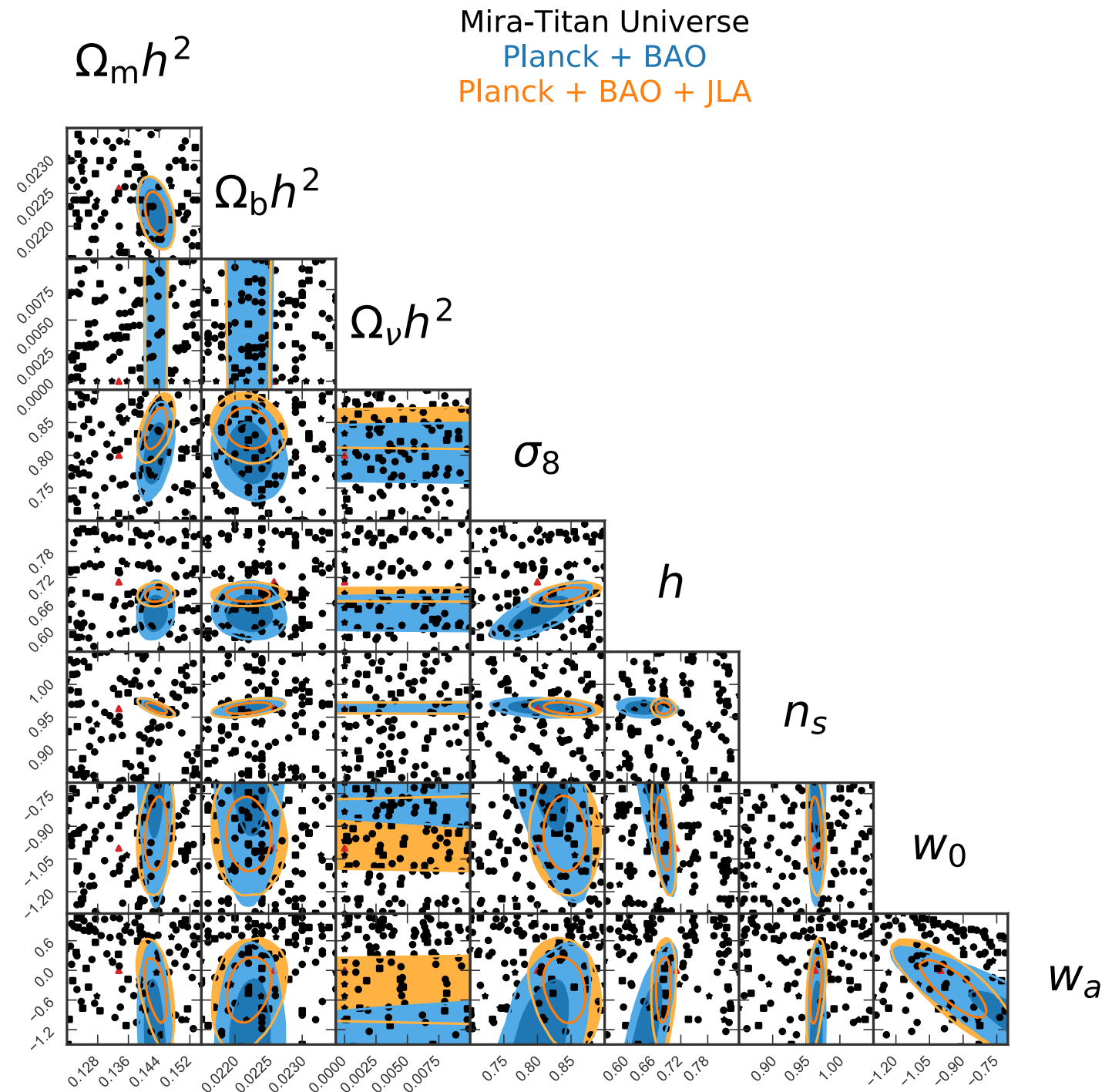
- Use DES+WISE to identify OIR counterparts near SPT cluster candidates
- Enables  $\sim 1.5x$  more clusters to lower detection SNR
- Klein+18, Klein+19



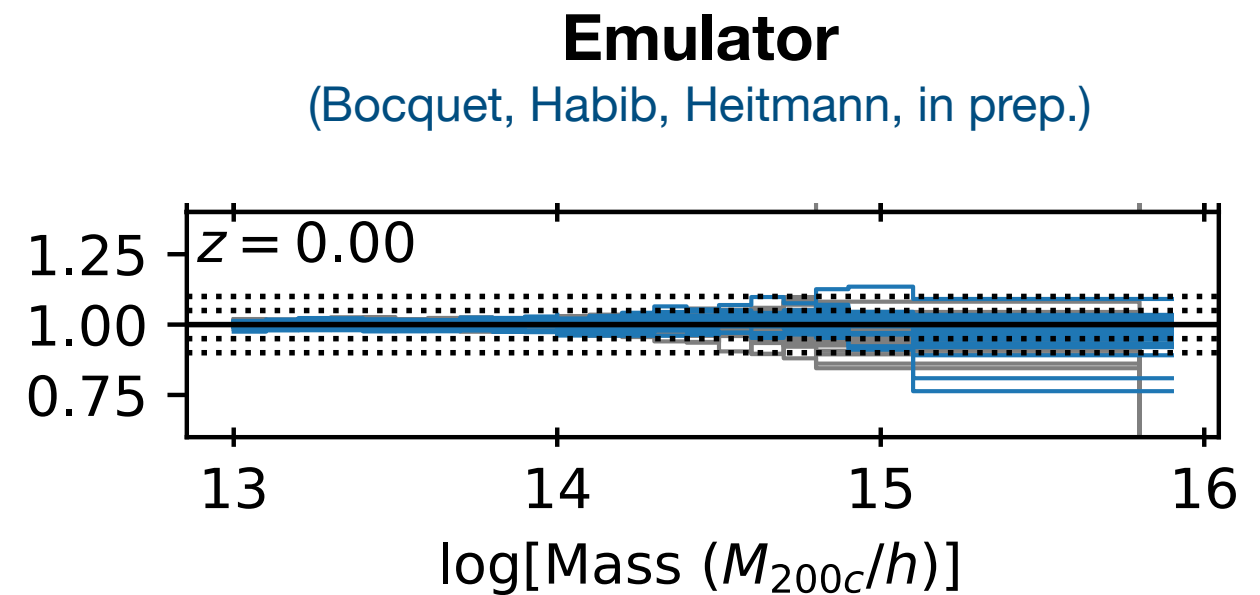
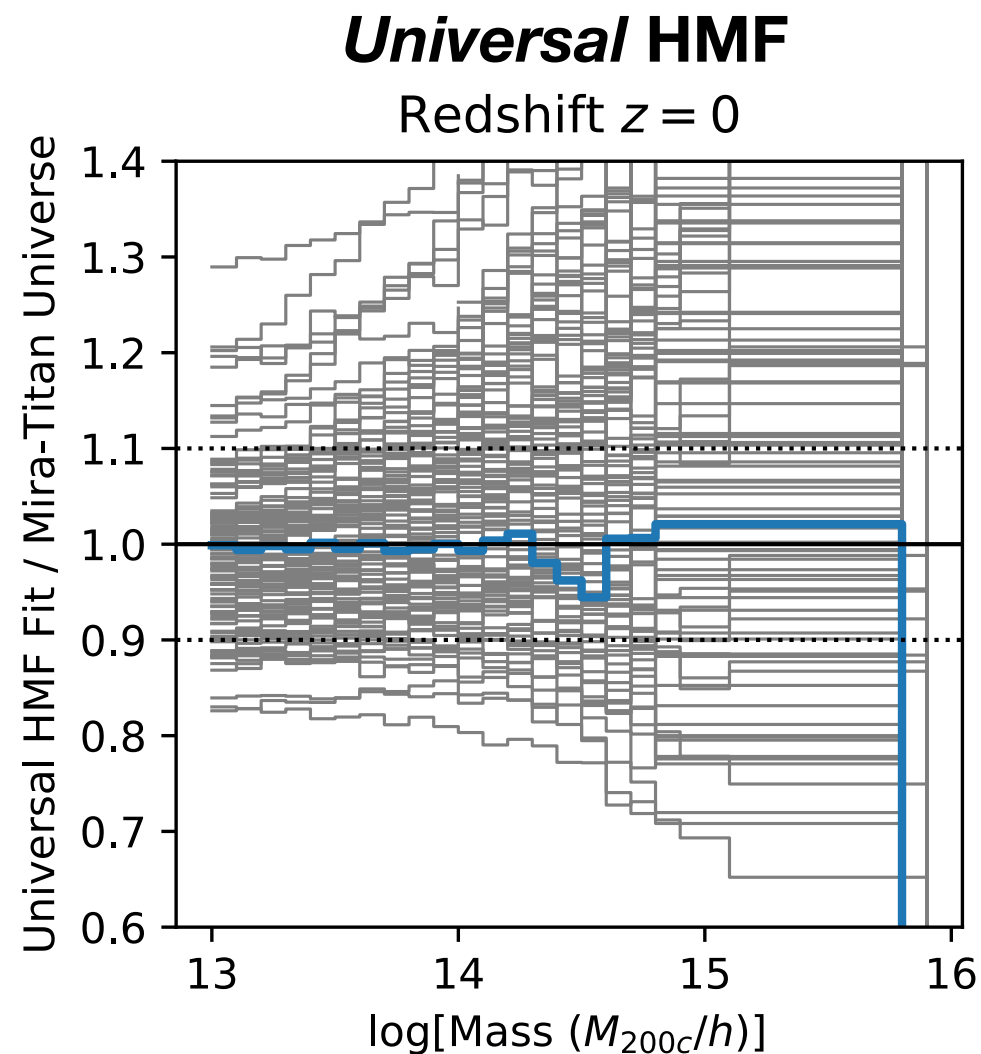
# Cosmology Dependence of Halo Mass Function



- Current “universal HMF” approach: extrapolate cosmology dependence
- Better: Use emulators to interpolate between numerical simulations of different cosmologies  
(Aemulus: McClintock+18, Dark Quest: Nishimichi+19)
- *Mira-Titan Universe*: first emulator suite to include massive neutrinos and dynamical dark energy  
(Heitmann+16)
- Use 111  $(2.1 \text{ Gpc})^3$  and  $(5 \text{ Gpc})^3$  simulations covering 8 cosmological parameters and interpolate using Gaussian process  
(Bocquet+ to be submitted)



# The Need for an HMF Emulator: Extreme example for $w_0w_a\text{CDM} + \Sigma m_\nu$



# Summary

- Data-driven cosmology from SPT galaxy clusters
  - Multi-observable modeling framework
  - Weak-lensing mass calibration
- WL sample is expanding thanks to the Dark Energy Survey, HST programs, and CMB lensing
- SPTpol cluster catalogs being published
  - Optical follow-up of SPT-3G high- $z$  clusters started tonight!
- HMF emulation
- Exciting times ahead!



# Backup Slides

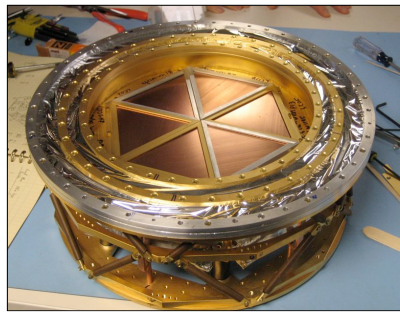
# The South Pole Telescope (SPT)

10-meter sub-mm quality  
wavelength telescope

95, 150, 220 GHz and  
1.6, 1.2, 1.0 arcmin resolution

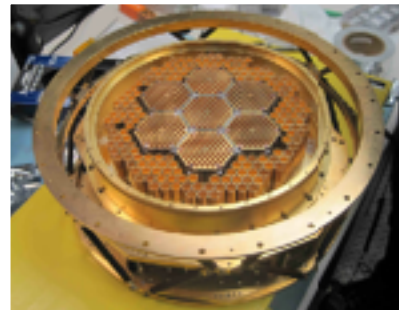
## 2007: SPT-SZ

960 detectors  
95, 150, 220 GHz



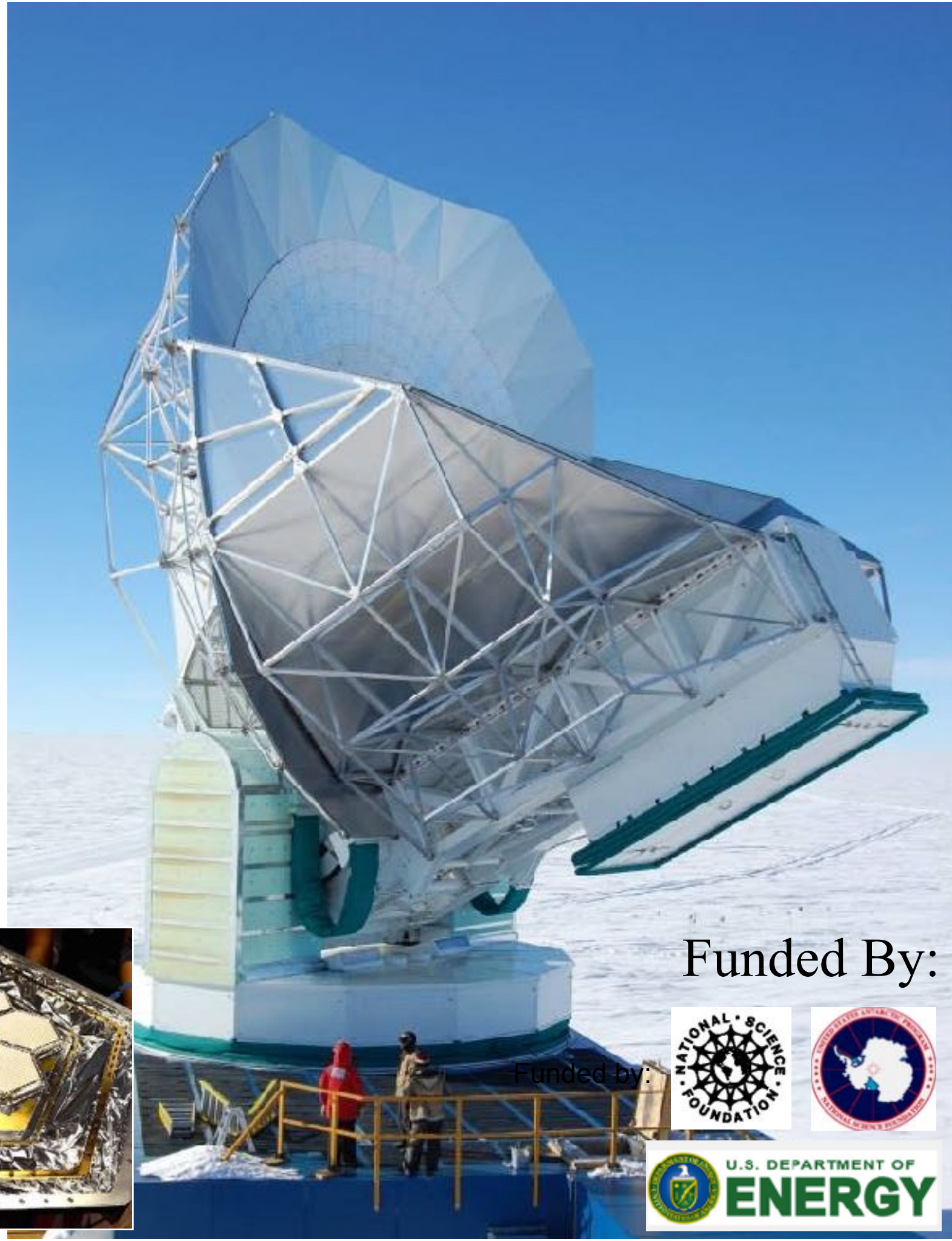
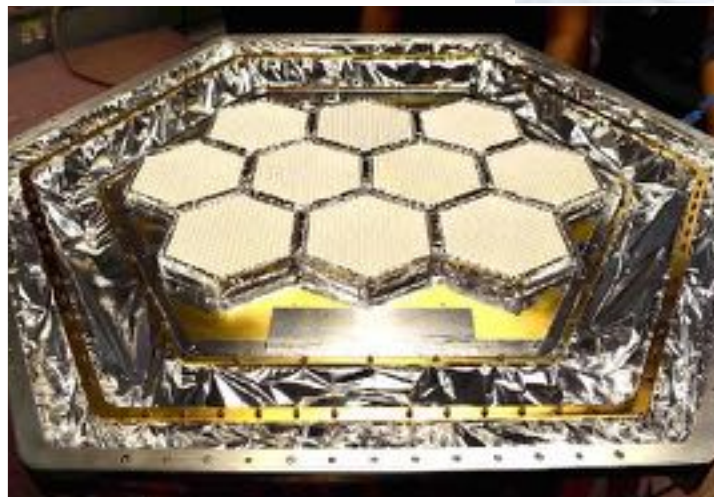
## 2012: SPTpol

1600 detectors  
90, 150 GHz  
**+Polarization**



## 2016: SPT-3G

~16,200 detectors  
95, 150, 225 GHz  
**+Polarization**



Funded By:





# Weak-Lensing Bias and Scatter

Bocquet et al. [2019ApJ...878...55B](#)

- WL is a biased mass estimator because we fit an NFW profile
- Simulation calibration:
  - NFW profile mismatch
  - Miscentering
  - Correlated LSS
- Other systematics:
  - Cluster member contamination
  - Shear and photo-z bias
- We are currently limited by the number of WL clusters, but that will change!

| Effect                                       | Impact on Mass     |                    |
|----------------------------------------------|--------------------|--------------------|
|                                              | Megacam            | HST                |
| WL mass bias                                 | 0.938              | 0.81 – 0.92        |
| Intrinsic scatter                            | 0.214              | (0.26 – 0.42)      |
| $\Delta$ (intrinsic scatter)                 | 0.04               | 0.021 – 0.055      |
| Uncorr. LSS scatter [ $M_\odot$ ]            | $9 \times 10^{13}$ | $8 \times 10^{13}$ |
| $\Delta$ (Uncorr. LSS scatter) [ $M_\odot$ ] | $10^{13}$          | $10^{13}$          |
| Mass modeling uncertainty                    | 4.4%               | 5.8 – 6.1%         |
| Systematic measurement uncert.               | 3.5%               | 7.2%               |
| Total systematic uncertainty                 | 5.6%               | 9.2 – 9.4%         |

**19 clusters    13 clusters**



# Multi-Observable – Mass Relation

## Mean relations

**SZ**  $\langle \ln \zeta \rangle = \ln A_{\text{SZ}} + B_{\text{SZ}} \ln \left( \frac{M_{500c} h_{70}}{4.3 \times 10^{14} M_{\odot}} \right) + C_{\text{SZ}} \ln \left( \frac{E(z)}{E(0.6)} \right)$  (1)

**X-ray**  $\ln \left( \frac{M_{500c} h_{70}}{8.37 \times 10^{13} M_{\odot}} \right) = \ln A_{Y_X} + B_{Y_X} \langle \ln Y_X \rangle - B_{Y_X} \ln \left( \frac{h_{70}^{5/2}}{3 \times 10^{14} M_{\odot} \text{keV}} \right) - C_{Y_X} \ln E(z)$  (2)

**WL**  $\langle \ln M_{\text{WL}} \rangle = \ln b_{\text{WL}} + \ln M_{500c}$  (3)

## Covariance matrix

$$\Sigma_{\text{multi-obs}} = \begin{pmatrix} \sigma_{\ln \zeta}^2 & \rho_{\text{SZ-WL}} \sigma_{\ln \zeta} \sigma_{\text{WL}} & \rho_{\text{SZ-X}} \sigma_{\ln \zeta} \sigma_{\ln Y_X} \\ \rho_{\text{SZ-WL}} \sigma_{\ln \zeta} \sigma_{\text{WL}} & \sigma_{\text{WL}}^2 & \rho_{\text{WL-X}} \sigma_{\text{WL}} \sigma_{\ln Y_X} \\ \rho_{\text{SZ-X}} \sigma_{\ln \zeta} \sigma_{\ln Y_X} & \rho_{\text{WL-X}} \sigma_{\text{WL}} \sigma_{\ln Y_X} & \sigma_{\ln Y_X}^2 \end{pmatrix} \quad (4)$$

## Multi-obs relation

$$P \left( \begin{bmatrix} \ln \zeta \\ \ln M_{\text{WL}} \\ \ln Y_X \end{bmatrix} | M, z, \mathbf{p} \right) = \mathcal{N} \left( \begin{bmatrix} \langle \ln \zeta \rangle(M, z, \mathbf{p}) \\ \langle \ln M_{\text{WL}} \rangle(M, z, \mathbf{p}) \\ \langle \ln Y_X \rangle(M, z, \mathbf{p}) \end{bmatrix}, \Sigma_{\text{multi-obs}} \right)$$

**3 + 3 + 1 parameters for mean relations**

**3 + 3 parameters for covariance matrix (correlated intrinsic scatter)**

# Likelihood Function in Observable Space



Poisson likelihood for cluster abundance

**Selection**  
 $x_i > 5, z > 0.25$

$$\ln \mathcal{L}(\vec{p}) = \sum_i \ln \frac{dN(\xi, z, \vec{p})}{d\xi dz} \Big|_{\xi_i, z_i} - \iint d\xi dz \Theta_{\text{survey}} \frac{dN(\xi, z, \vec{p})}{d\xi dz} + \sum_j \underbrace{P(Y_X, g_t | \xi_j, z_j, \vec{p})}_{\text{Mass calibration}} \Big|_{Y_{X_j}, g_{tj}}$$

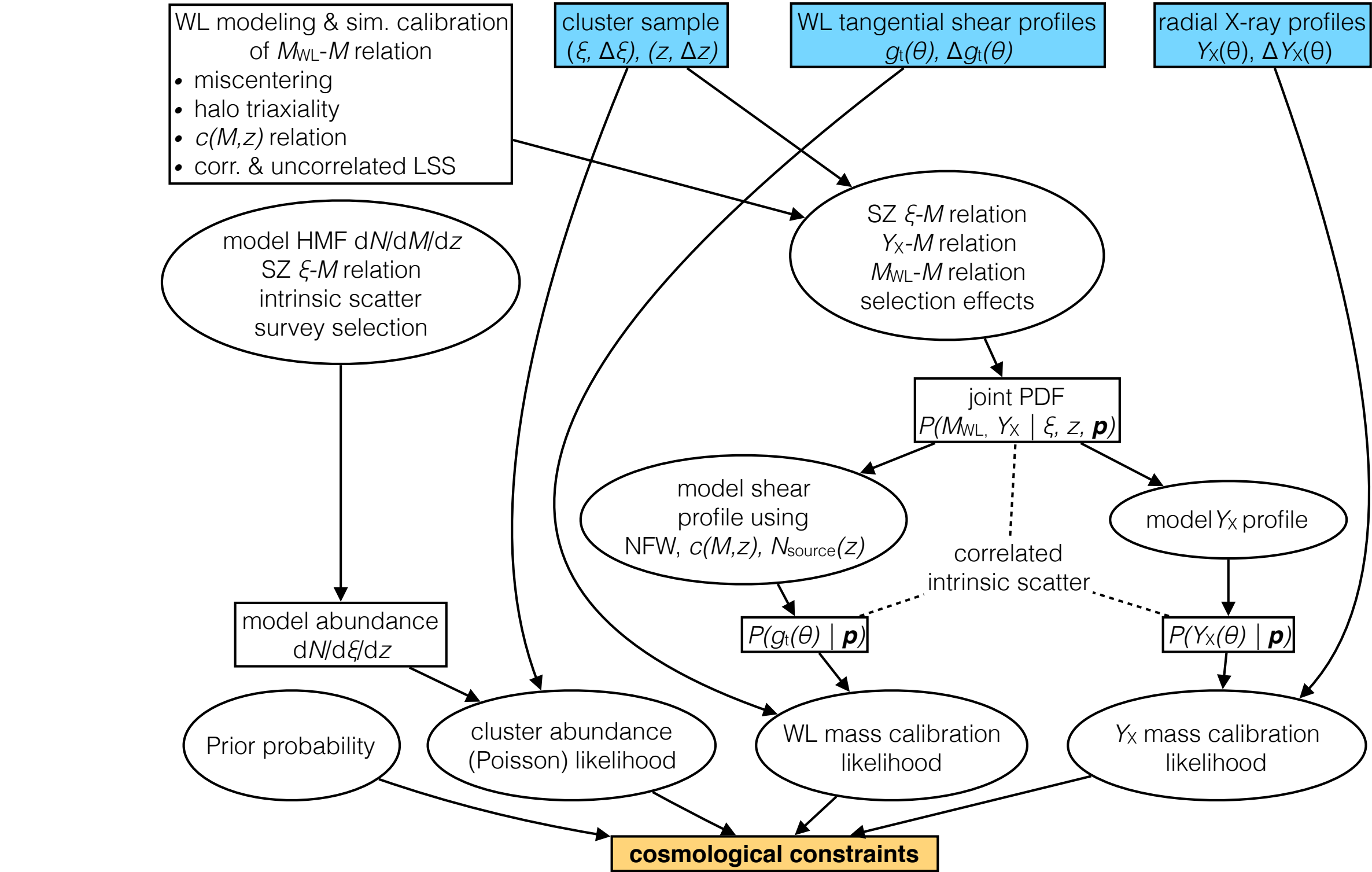
**Total predicted number**

$$\frac{dN(\xi, z | \mathbf{p})}{d\xi dz} = \iint dM d\zeta \left[ P(\xi | \zeta) P(\zeta | M, z, \mathbf{p}) \frac{dN(M, z | \mathbf{p})}{dM dz} \Omega(z, \mathbf{p}) \right]$$

$$\underbrace{P(Y_X^{\text{obs}}, g_t^{\text{obs}} | \xi, z, \mathbf{p})}_{\text{Total predicted number}} = \iiint dM d\zeta dY_X dM_{\text{WL}} \left[ P(Y_X^{\text{obs}} | Y_X) P(g_t^{\text{obs}} | M_{\text{WL}}) P(\xi | \zeta) P(\zeta, Y_X, M_{\text{WL}} | M, z, \mathbf{p}) P(M | z, \mathbf{p}) \right]$$

# Analysis workflow

Bocquet+ (arXiv: 1812.01679)





# Pipeline Validation, Parameters, and Priors

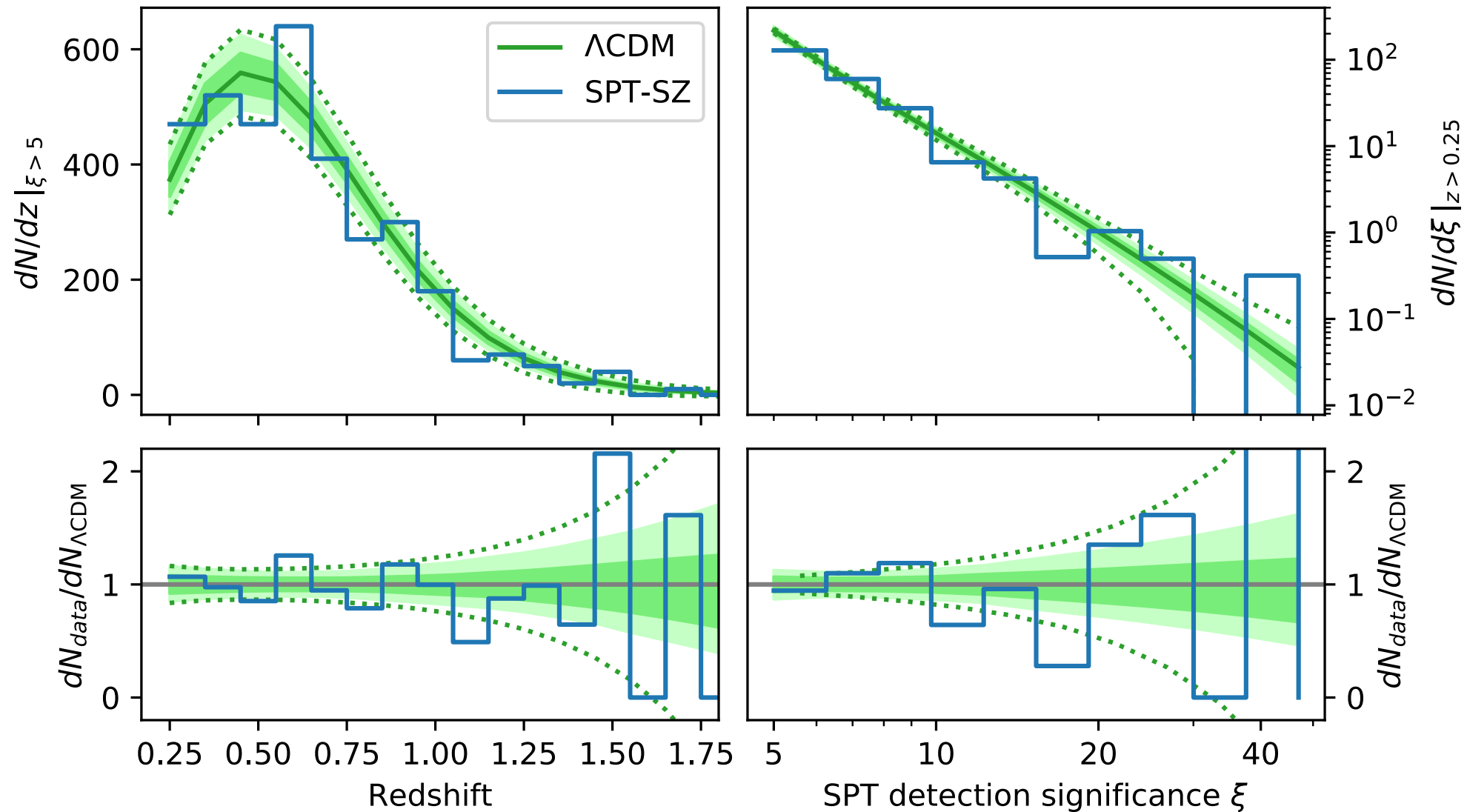
Bocquet et al. [2019ApJ...878...55B](#)

- Pipeline validation against mocks:
  - Draw halos from HMF
  - Assign multivariate observable distribution
  - Mock creation is easier than actual analysis (otherwise, this test is pointless!)
- Any remaining bias in analysis pipeline is small compared to uncertainty from real data
- Validate zero point (HMF) against independent implementations

| Parameter                           | Prior                                                       |
|-------------------------------------|-------------------------------------------------------------|
| Cosmological                        |                                                             |
| $\Omega_m$                          | $\mathcal{U}(0.05, 0.6), \Omega_m(z > 0.25) > 0.156$        |
| $\Omega_b h^2$                      | $\mathcal{U}(0.020, 0.024)$                                 |
| $\Omega_\nu h^2$                    | $\mathcal{U}(0, 0.01)$                                      |
| $\Omega_k$                          | fixed (0)                                                   |
| $A_s$                               | $\mathcal{U}(10^{-10}, 10^{-8})$                            |
| $h$                                 | $\mathcal{U}(0.55, 0.9)$                                    |
| $n_s$                               | $\mathcal{U}(0.94, 1.00)$                                   |
| $w$                                 | fixed (-1) or $\mathcal{U}(-2.5, -0.33)$                    |
| Optical depth to reionization       |                                                             |
| $\tau$                              | fixed or $\mathcal{U}(0.02, 0.14)$                          |
| SZ scaling relation                 |                                                             |
| $A_{SZ}$                            | $\mathcal{U}(1, 10)$                                        |
| $B_{SZ}$                            | $\mathcal{U}(1, 2.5)$                                       |
| $C_{SZ}$                            | $\mathcal{U}(-1, 2.5)$                                      |
| $\sigma_{\ln \zeta}$                | $\mathcal{U}(0.01, 0.5) (\times \mathcal{N}(0.13, 0.13^2))$ |
| X-ray $Y_X$ scaling relation        |                                                             |
| $A_{Y_X}$                           | $\mathcal{U}(3, 10)$                                        |
| $B_{Y_X}$                           | $\mathcal{U}(0.3, 0.9)$                                     |
| $C_{Y_X}$                           | $\mathcal{U}(-1, 0.5)$                                      |
| $\sigma_{\ln Y_X}$                  | $\mathcal{U}(0.01, 0.5)$                                    |
| $d \ln M_g / d \ln r$               | $\mathcal{U}(0.4, 1.8) \times \mathcal{N}(1.12, 0.23^2)$    |
| WL modeling                         |                                                             |
| $\delta_{WL, \text{bias}}$          | $\mathcal{U}(-3, 3) \times \mathcal{N}(0, 1)$               |
| $\delta_{\text{Megacam}}$           | $\mathcal{U}(-3, 3) \times \mathcal{N}(0, 1)$               |
| $\delta_{\text{HST}}$               | $\mathcal{U}(-3, 3) \times \mathcal{N}(0, 1)$               |
| $\delta_{WL, \text{scatter}}$       | $\mathcal{U}(-3, 3) \times \mathcal{N}(0, 1)$               |
| $\sigma_{WL, LSS_{\text{Megacam}}}$ | $\mathcal{U}(-3, 3) \times \mathcal{N}(0, 1)$               |
| $\sigma_{WL, LSS_{\text{HST}}}$     | $\mathcal{U}(-3, 3) \times \mathcal{N}(0, 1)$               |
| Correlated scatter                  |                                                             |
| $\rho_{SZ-WL}$                      | $\mathcal{U}(0, 1)$                                         |
| $\rho_{SZ-X}$                       | $\mathcal{U}(0, 1)$                                         |
| $\rho_{X-WL}$                       | $\mathcal{U}(0, 1)$                                         |
|                                     | $\det(\Sigma) > 0$                                          |

# Goodness of Fit Test: Passed

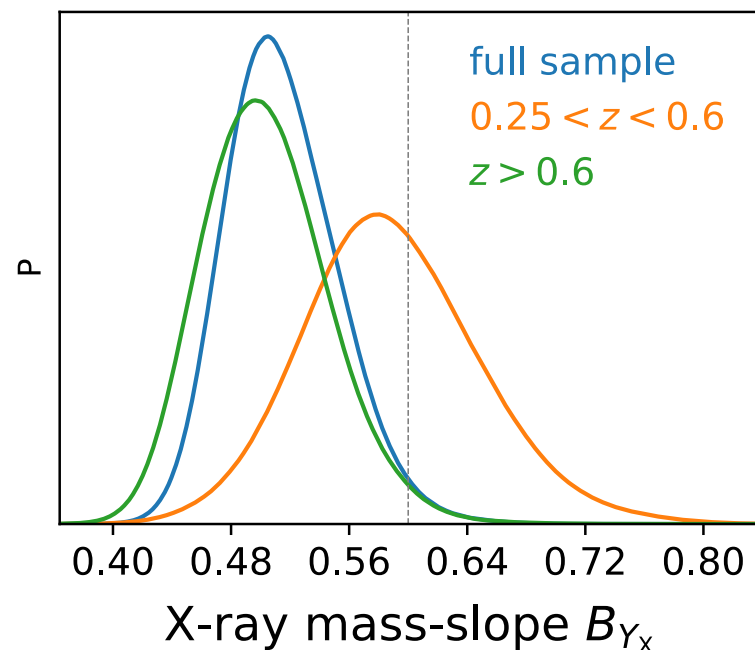
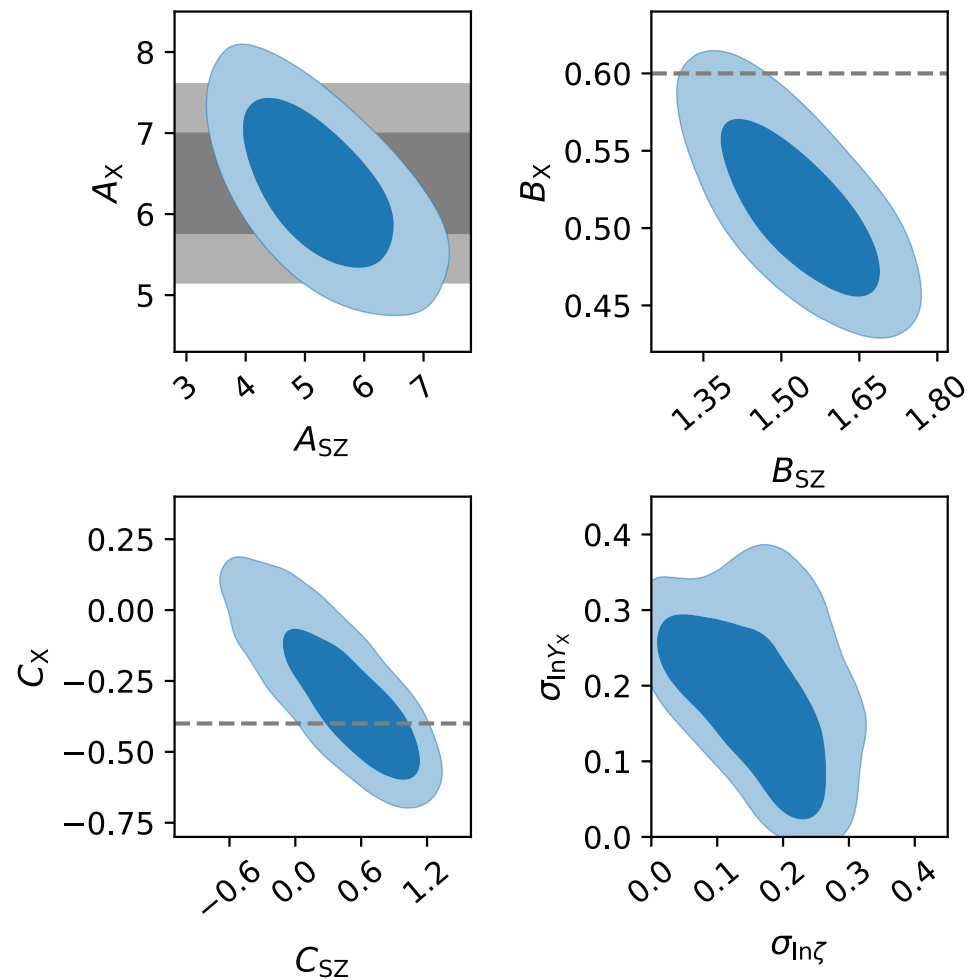
Bocquet et al. [2019ApJ...878...55B](#)



- Number counts test statistic (Kaastra 17)
  - $C(\text{model}) = 439.8 \pm 26.8$
  - $C(\text{data}) = 449.3$

# X-ray Scaling Relation

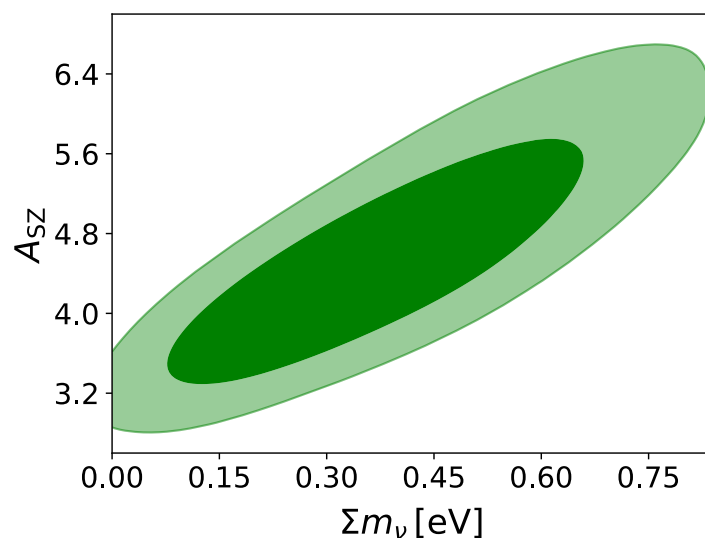
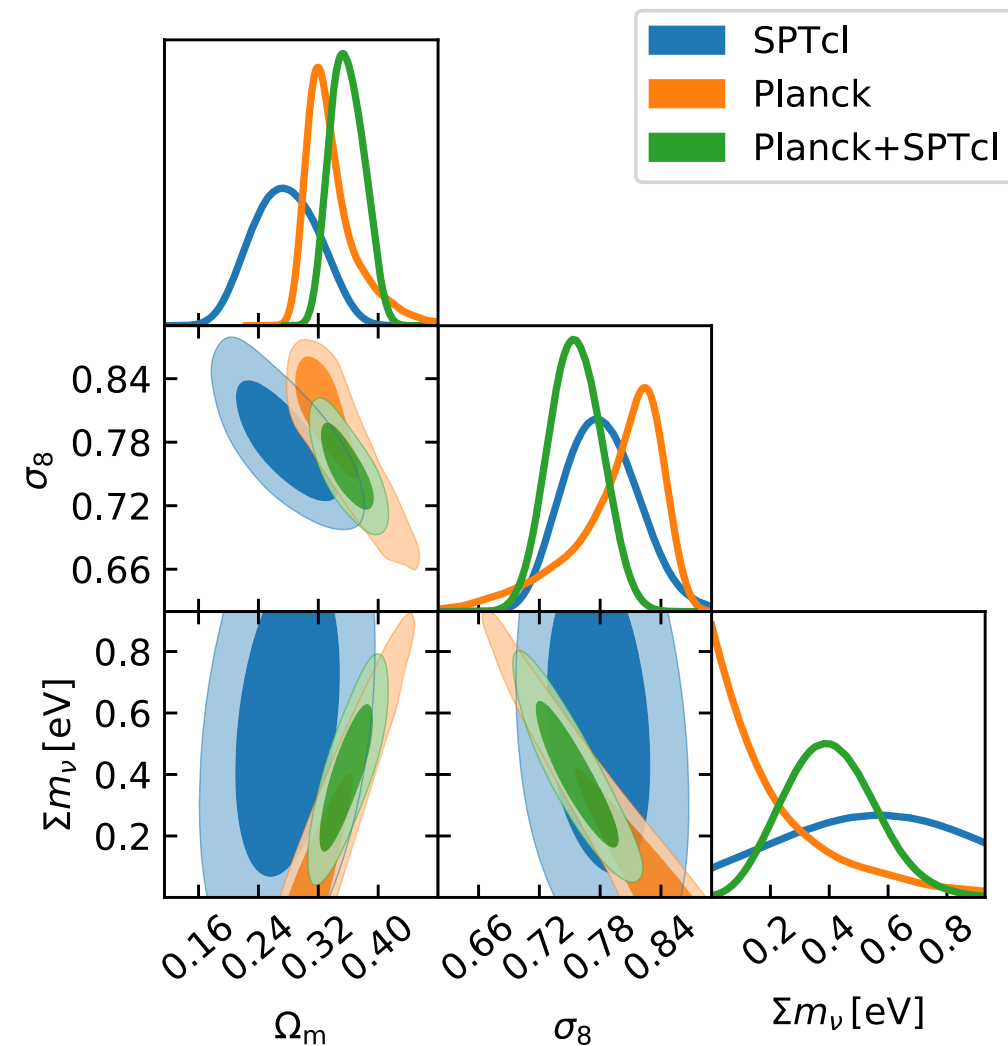
Bocquet et al. [2019ApJ...878...55B](#)



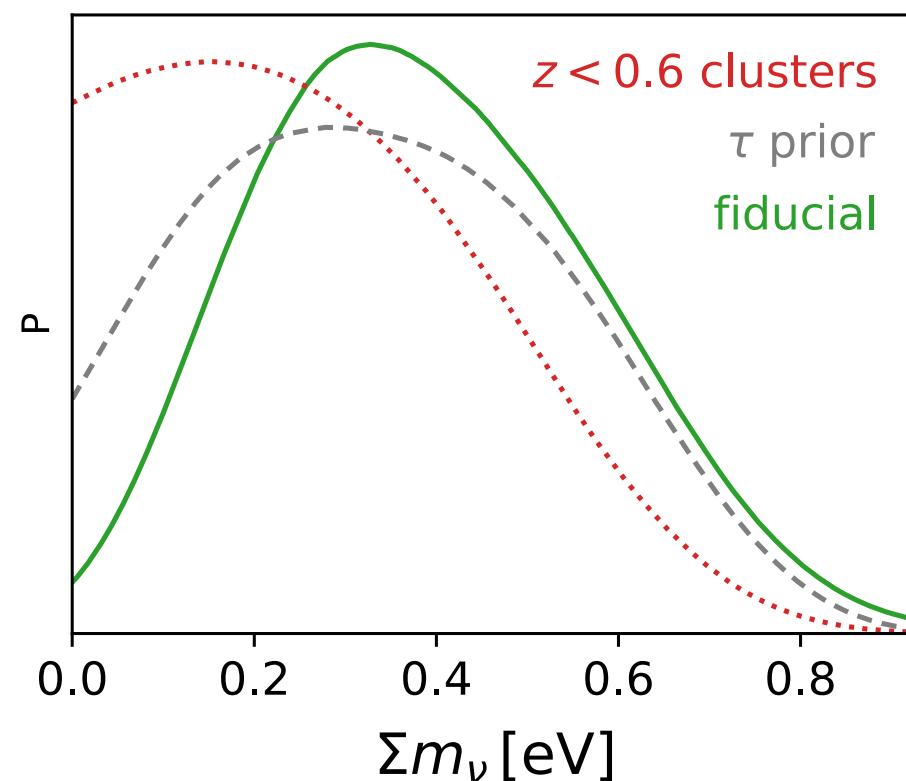
- Constraints on X-ray scaling relations as a “byproduct”
- Self-similar model prediction if non-thermal pressure support is negligible
- Redshift evolution is self-similar
- Mass evolution is steeper than self-similar
  - Low-redshift half ( $0.25 < z < 0.6$ ) in  $< 1 \sigma$  agreement with the standard self-similar evolution
  - High-redshift half ( $z > 0.6$ ) shows signs of departure at  $\sim 3 \sigma$  level
- Very similar story when using  $M_{\text{gas}}$  instead of  $Y_X$
- Also consistent with XMM results for SPT clusters (Bulbul et al. 2018)

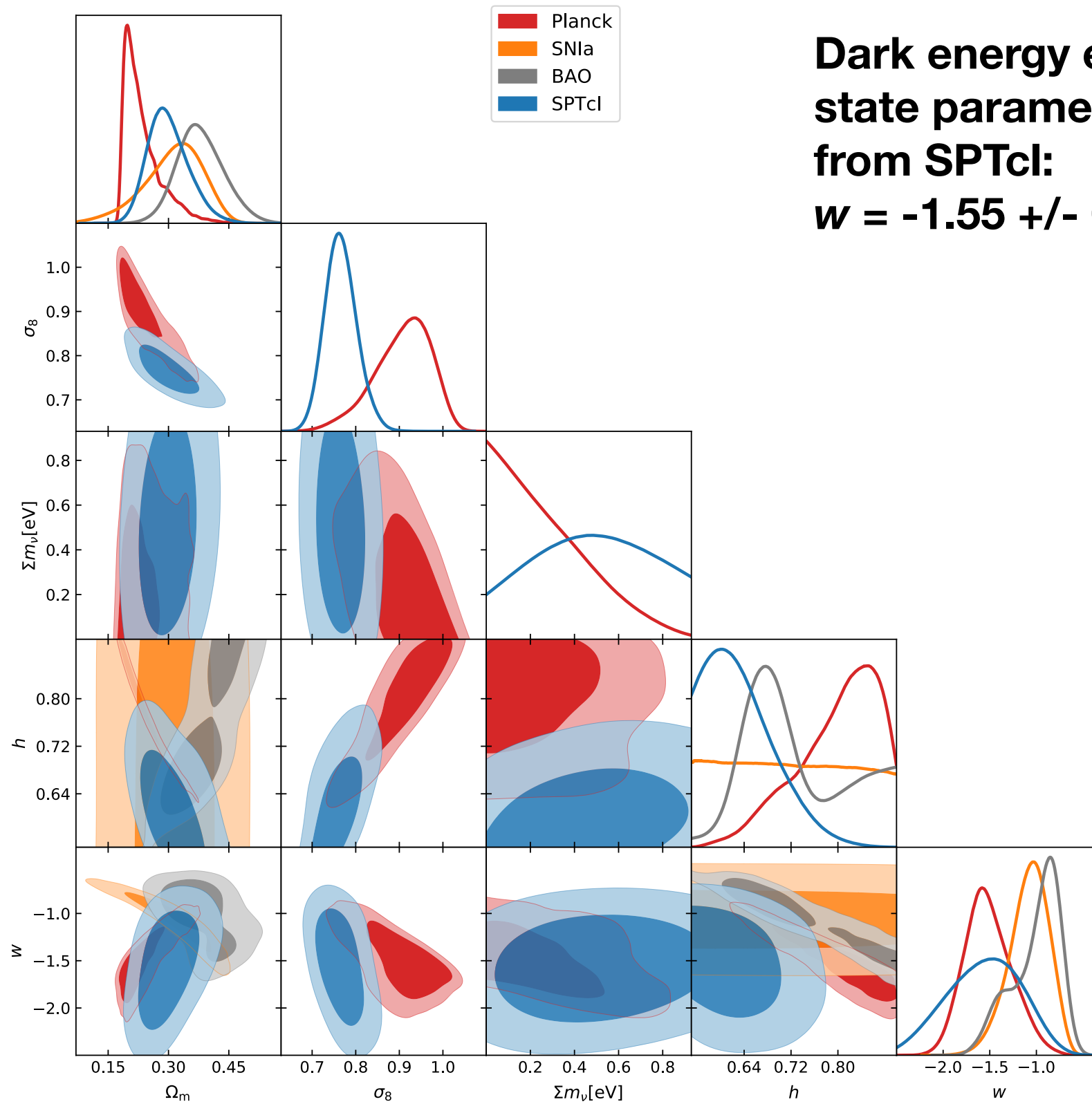
# Neutrino Masses

Bocquet et al. [2019ApJ...878...55B](#)

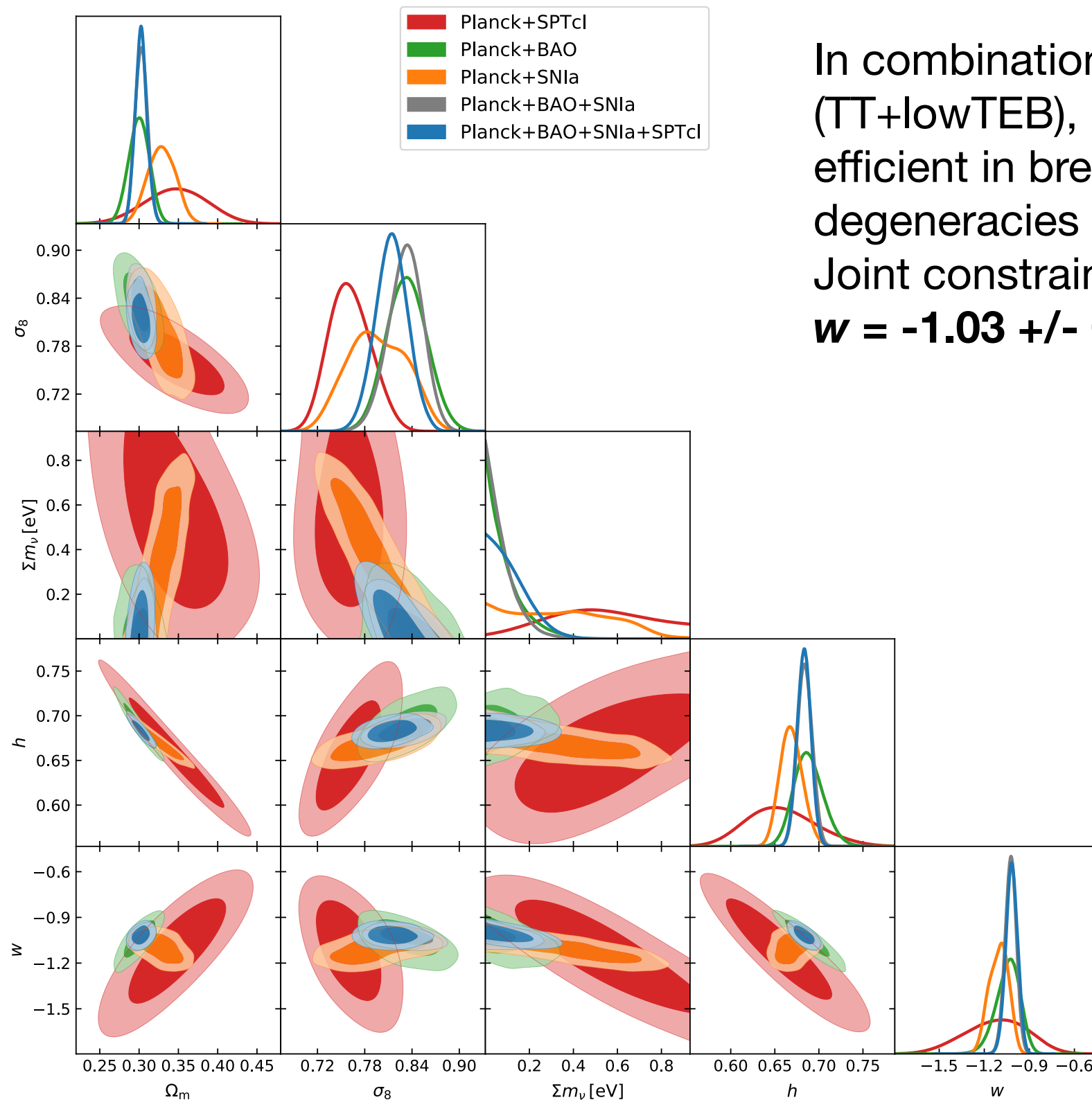


- Combination with Planck primary CMB measurements yields  $2\sigma$  preference for non-zero sum of neutrino masses
- Again, limited by mass calibration uncertainties
- Using  $\tau$  prior from Planck 2018 gives  $1.7\sigma$  preference
- Using only the  $z < 0.6$  cluster sample gives no preference for non-zero sum of neutrino masses





**Dark energy equation of state parameter from SPTcl:**  
 $w = -1.55 \pm 0.41$



In combination with Planck (TT+lowTEB), SPTcl is not as efficient in breaking degeneracies as BAO or SNla. Joint constraint:  
 **$w = -1.03 \pm 0.04$**